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Infinitely many solutions for the prescribed Q-curvature problem in the null case

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Abstract

Given a compact Riemannian manifold (M, g) of even dimension, we provide sufficient conditions for the existence of infinitely many metrics within the conformal class of g that realize a prescribed Q-curvature.

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